

MPI – Codes, etc

Beowulf Howto

1. `modify /etc/hosts`
2. Export all home directories, in `/etc/exports`

```
/home    node02(rw)
```

For each new user, update:

```
scp /etc/passwd node02:/etc
scp /etc/shadow node02:/etc
scp /etc/group node02:/etc
```

```
echo "Enabling ssh communication..."
cp -r /root/.ssh /home/$1
chown -R $1:$2 /home/$1/.ssh
```

Examples in MPI

Compiling and Execution

Ver 1

```
mpicc -o program_name program_name.c
```

Or, in case of panic:

```
cc -o program_name program_name.c  
-I/usr/local/mpich-1.2.5/include  
-L/usr/local/mpich-1.2.5/lib
```

To execute a program on n processes:

```
mpirun -np n program_name
```

Compiling and Execution

Ver 2

```
mpicc -o program_name program_name.c
```

Or, in case panic:

```
cc -o program_name program_name.c  
-I/usr/local/mpich2-1.2/include  
-L/usr/local/mpich2-1.2/lib
```

To execute a program on n processes:

```
mpd & // only at the beginning of the session  
mpiexec -n num_proc program_name  
mpdallexit // at the end of the session
```

Debugging tips

- Run the program with one process just like a normal sequential program
- Run the program on 2-4 processes. Check sending of messages (correct recipient, tags, etc.)
- Run the program on 2-4 processors

```
* See Chapter 3, pp. 41 & ff in PPMPI.
```

```
*/
```

```
#include <stdio.h>
#include <string.h>
#include "mpi.h"
```

```
main(int argc, char* argv[]) {
    int    my_rank;      /* rank of process */
    int    p;           /* number of processes */
    int    source;      /* rank of sender */
    int    dest;        /* rank of receiver */
    int    tag = 0;     /* tag for messages */
    char   message[100]; /* storage for message */
    MPI_Status status;  /* return status for */
                                /* receive */

    /* Start up MPI */
    MPI_Init(&argc, &argv);

    /* Find out process rank */
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    /* Find out number of processes */
    MPI_Comm_size(MPI_COMM_WORLD, &p);

    if (my_rank != 0) {
        /* Create message */
        sprintf(message, "Greetings from process %d!",
                my_rank);
        dest = 0;
        /* Use strlen+1 so that '\0' gets transmitted */
        MPI_Send(message, strlen(message)+1, MPI_CHAR,
                 dest, tag, MPI_COMM_WORLD);
    } else { /* my_rank == 0 */
        for (source = 1; source < p; source++) {
            MPI_Recv(message, 100, MPI_CHAR, source, tag,
                    MPI_COMM_WORLD, &status);
            printf("%s\n", message);
        }
    }

    /* Shut down MPI */
    MPI_Finalize();
} /* main */
```

Hello World!

A simple ping

```
#include "mpi.h"
#include <stdio.h>

int main(argc,argv)
int argc;
char *argv[]; {
int numtasks, rank, dest, source, rc, count, tag=1;
char inmsg, outmsg='x';
MPI_Status Stat;

MPI_Init(&argc,&argv);
MPI_Comm_size(MPI_COMM_WORLD, &numtasks);
MPI_Comm_rank(MPI_COMM_WORLD, &rank);

if (rank == 0) {
    dest = 1;
    source = 1;
    rc = MPI_Send(&outmsg, 1, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
    rc = MPI_Recv(&inmsg, 1, MPI_CHAR, source, tag, MPI_COMM_WORLD, &Stat);
}
else if (rank == 1) {
    dest = 0;
    source = 0;
    rc = MPI_Recv(&inmsg, 1, MPI_CHAR, source, tag, MPI_COMM_WORLD, &Stat);
    rc = MPI_Send(&outmsg, 1, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
}
rc = MPI_Get_count(&Stat, MPI_CHAR, &count);
printf("Task %d: Received %d char(s) from task %d with tag %d \n",
        rank, count, Stat.MPI_SOURCE, Stat.MPI_TAG);
MPI_Finalize();
}
```



```

#include <mpi.h>
#include <stdio.h>

#define MAXSIZE 10

int main(int argc, char** argv)
{
    int myid, numprocs;
    int data[MAXSIZE], i, x, low, high, myresult, result, result_temp;
    int dest, source;

    MPI_Init(&argc, &argv);
    MPI_Status status;
    MPI_Comm_size(MPI_COMM_WORLD, &numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD, &myid);

    result = 0;
    myresult = 0;

    // Inizializzo...(ogni "processo" vedrà la propria porzione inizializzata)
    for (i=0; i<MAXSIZE;i++)
        data[i] = i;
    }

    // Individuo la mia porzione
    x = MAXSIZE/numprocs;
    low = myid * x;
    high = low + x;

    // Calcolo il mio risultato (anche il processo 0 lo farà')
    for (i=low; i<high; i++)
        myresult = myresult + data[i];

    if (myid == 0){
        result = myresult;
        for (source=1; source<numprocs; source++){
            MPI_Recv(&myresult, 1, MPI_INT, source, 0, MPI_COMM_WORLD, &status);
            result = result + myresult;
        }
    }
    else
        MPI_Send(&myresult, 1, MPI_INT, 0, 0, MPI_COMM_WORLD);

    if (myid ==0)
        printf("La somma è %d.\n", result);

    MPI_Finalize();
    exit(0);
}

```

Vector sum (without Broadcast and Reduce)

«Global» variables!

Let's get timings!

- To "take" the execution time of an MPI program we can use the timer function `MPI_Wtime (void)`
- First step: Synchronize all processes via a call to `MPI_Barrier()`

- Get initial time with

```
start=MPI_Wtime();
```

- At the end of the code, call `MPI_Barrier()` to re-synchronize processes
- Take final time with

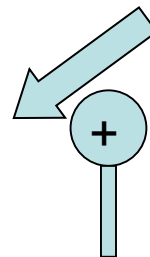
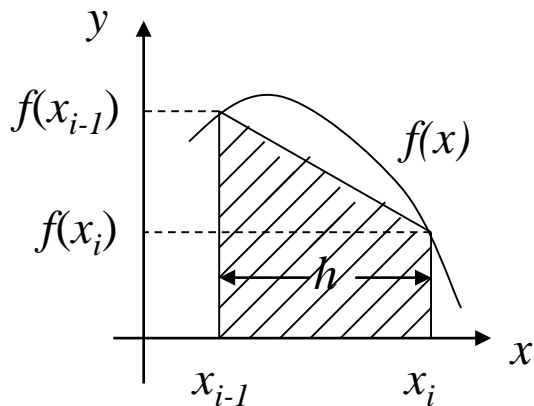
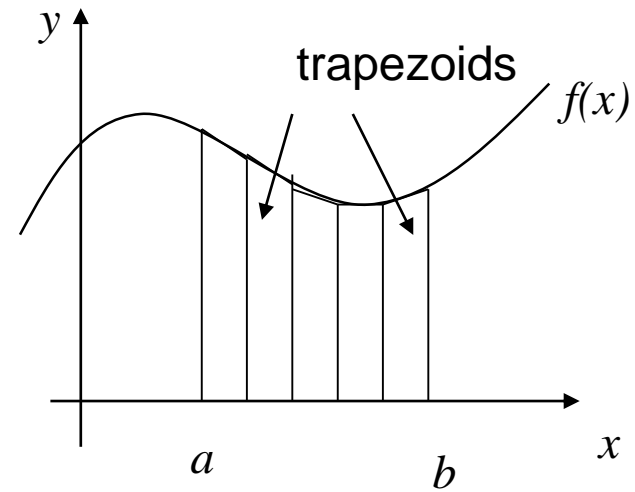
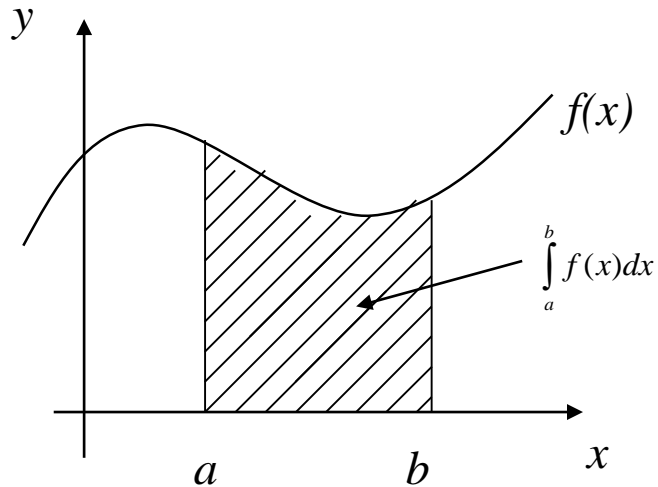
```
finish=MPI_Wtime();
```

- Let only process 0 print the elapsed time:

```
printf("Elapsed time is = %f seconds\n", finish-start);
```

- `MPI_Wtime()` returns the **wall-clock time**, that is includes also system time, etc

Example: Numerical Integration



Example: Numerical Integration

- Trapezoid rule
- Each rectangle has base $h=(b-a)/n$
- The trapezium has left-most base $[a, a+h]$, the next $[a+h, a+2h]$, the next $[a+2h, a+3h]$, etc
- Let's denote $x_i=a+ih, i=0,\dots,n$
- So, the left side of each trapezoid is $f(x_{i-1})$, while the right is $f(x_i)$

Example: Numerical Integration

- The area of the i -th trapezoid is $\frac{1}{2} h[f(x_{i-1})+f(x_i)]$
- The approximation of the entire area will be the sum of the area of the trapezoids:

$$\begin{aligned} & \frac{1}{2} h[f(x_0)+f(x_1)] + \frac{1}{2} h [f(x_1)+f(x_2)] + \dots + \frac{1}{2} h [f(x_{n-1})+f(x_n)] = \\ & = h/2 [f(x_0) + 2f(x_1) + 2f(x_2) + \dots + f(x_n)] = \\ & = [f(x_0)/2 + f(x_n)/2 + f(x_1) + f(x_2) + \dots + f(x_{n-1})]h \end{aligned}$$

```

#include <stdio.h>

main() {
    float  integral;    /* Store result in integral    */
    float  a, b;        /* Left and right endpoints    */
    int    n;           /* Number of trapezoids        */
    float  h;           /* Trapezoid base width        */
    float  x;
    int    i;

    float  f(float x); /* Function we're integrating */

    printf("Enter a, b, and n\n");
    scanf("%f %f %d", &a, &b, &n);

    h = (b-a)/n;
    integral = (f(a) + f(b))/2.0;
    x = a;
    for (i = 1; i <= n-1; i++) {
        x = x + h;
        integral = integral + f(x);
    }
    integral = integral*h;

    printf("With n = %d trapezoids, our estimate\n",
           n);
    printf("of the integral from %f to %f = %f\n",
           a, b, integral);
} /* main */

float f(float x) {
    float return_val;
    /* Calculate f(x). Store calculation in return_val. */

    return_val = x*x;
    return return_val;
} /* f */

```

Sequential version

Parallelization

- A possible method is to assign a portion of the interval $[a, b]$ for each process (data parallelism!)
- How does each process know the subinterval and how many trapezoids to use?
- **Natural solution:** the first process computes the first n/p trapezoids, the second the second n/p trapezoids, etc. (where p is the number of processes)

Parallelization

- Therefore, each process needs to know
 - The number of processes, p
 - Their rank
 - The entire integration interval $[a, b]$
 - The number of subintervals, n
- The first two information are provided by `MPI_Comm_size` and `MPI_Comm_rank`, the latter two should be provided by the user.
- **Last observation:** how are the partial sums added together for each process?
- **Possible Solution:** Each process sends its partial sum to process 0, and this performs the sum.


```

#include <stdio.h>

/* We'll be using MPI routines, definitions, etc. */
#include "mpi.h"

main(int argc, char** argv) {
    int    my_rank; /* My process rank */
    int    p;      /* The number of processes */
    float  a = 0.0; /* Left endpoint */
    float  b = 1.0; /* Right endpoint */
    int    n = 1024; /* Number of trapezoids */
    float  h;      /* Trapezoid base length */
    float  local_a; /* Left endpoint my process */
    float  local_b; /* Right endpoint my process */
    int    local_n; /* Number of trapezoids for my calculation */
    float  integral; /* Integral over my interval */
    float  total;   /* Total integral */
    int    source;  /* Process sending integral */
    int    dest = 0; /* All messages go to 0 */
    int    tag = 0;
    MPI_Status status;

    /* Let the system do what it needs to start up MPI */
    MPI_Init(&argc, &argv);

    /* Get my process rank */
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    /* Find out how many processes are being used */
    MPI_Comm_size(MPI_COMM_WORLD, &p);

    h = (b-a)/n; /* h is the same for all processes */
    local_n = n/p; /* So is the number of trapezoids */

    /* Length of each process' interval of
     * integration = local_n*h. So my interval
     * starts at: */
    local_a = a + my_rank*local_n*h;
    local_b = local_a + local_n*h;
    integral = Trap(local_a, local_b, local_n, h);

    /* Add up the integrals calculated by each process */
    if (my_rank == 0) {
        total = integral;
        for (source = 1; source < p; source++) {
            MPI_Recv(&integral, 1, MPI_FLOAT, source, tag,
                    MPI_COMM_WORLD, &status);
            total = total + integral;
        }
    } else {
        MPI_Send(&integral, 1, MPI_FLOAT, dest,
                tag, MPI_COMM_WORLD);
    }

    /* Print the result */
    if (my_rank == 0) {
        printf("With n = %d trapezoids, our estimate\n",
              n);
        printf("of the integral from %f to %f = %f\n",
              a, b, total);
    }

    /* Shut down MPI */
    MPI_Finalize();
} /* main */

```

NB!

Each process (including 0) calculates the sum of the areas of the "local" trapezoids

Process 0 receives all (it has already its area!)

```

float Trap(
    float local_a    /* in */,
    float local_b    /* in */,
    int   local_n    /* in */,
    float h          /* in */) {

    float integral; /* Store result in integral */
    float x;
    int i;

    float f(float x); /* function we're integrating */

    integral = (f(local_a) + f(local_b))/2.0;
    x = local_a;
    for (i = 1; i <= local_n-1; i++) {
        x = x + h;
        integral = integral + f(x);
    }
    integral = integral*h;
    return integral;
} /* Trap */

```

← Area computation of local trapezoids

```

float f(float x) {
    float return_val;
    /* Calculate f(x). */
    /* Store calculation in return_val. */
    return_val = x*x;
    return return_val;
} /* f */

```

← Ex: $f(x) = x^2$

I / O

- The function $f(x)$ and the variables a , b and n well are "hardwired"
- $f(x)$ can be defined as a pointer function (or callback function) (home exercise)
- Although not a standard procedure, it is advisable that a process takes care of the I / O (for instance, process 0 sends the initial data, a , b and n to processes)

I/O

If for each process I execute:

```
scanf ("%f %f %d", &a, &b, &n);
```

What happens?

If for each process I execute:

```
printf ("%f %f %d", a, b, n);
```

What happens?

```

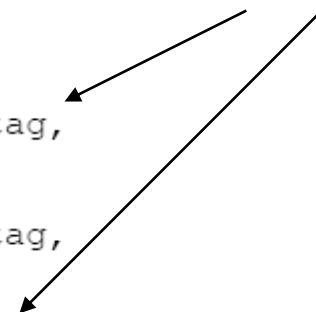
void Get_data(
    float*  a_ptr    /* out */,
    float*  b_ptr    /* out */,
    int*    n_ptr    /* out */,
    int     my_rank  /* in   */,
    int     p        /* in   */) {

    int source = 0;    /* All local variables used by */
    int dest;        /* MPI_Send and MPI_Recv      */
    int tag;
    MPI_Status status;

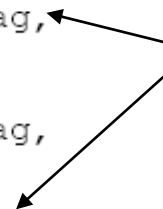
    if (my_rank == 0) {
        printf("Enter a, b, and n\n");
        scanf("%f %f %d", a_ptr, b_ptr, n_ptr);
        for (dest = 1; dest < p; dest++) {
            tag = 0;
            MPI_Send(a_ptr, 1, MPI_FLOAT, dest, tag,
                    MPI_COMM_WORLD);
            tag = 1;
            MPI_Send(b_ptr, 1, MPI_FLOAT, dest, tag,
                    MPI_COMM_WORLD);
            tag = 2;
            MPI_Send(n_ptr, 1, MPI_INT, dest, tag,
                    MPI_COMM_WORLD);
        }
    } else {
        tag = 0;
        MPI_Recv(a_ptr, 1, MPI_FLOAT, source, tag,
                MPI_COMM_WORLD, &status);
        tag = 1;
        MPI_Recv(b_ptr, 1, MPI_FLOAT, source, tag,
                MPI_COMM_WORLD, &status);
        tag = 2;
        MPI_Recv(n_ptr, 1, MPI_INT, source, tag,
                MPI_COMM_WORLD, &status);
    }
} /* Get_data */

```

Note different tags!!!



Note different tags!!!



Call to Get_data

```
/* Let the system do what it needs to start up MPI */
MPI_Init(&argc, &argv);

/* Get my process rank */
MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

/* Find out how many processes are being used */
MPI_Comm_size(MPI_COMM_WORLD, &p);

h = (b-a)/n; /* h is the same for all processes */
local_n = n/p; /* So is the number of trapezoids */

/* Length of each process' interval of
 * integration = local_n*h. So my interval
 * starts at: */
local_a = a + my_rank*local_n*h;
local_b = local_a + local_n*h;
integral = Trap(local_a, local_b, local_n, h);

/* Add up the integrals calculated by each process */
if (my_rank == 0) {
    total = integral;
    for (source = 1; source < p; source++) {
        MPI_Recv(&integral, 1, MPI_FLOAT, source, tag,
                MPI_COMM_WORLD, &status);
        total = total + integral;
    }
} else {
    MPI_Send(&integral, 1, MPI_FLOAT, dest,
            tag, MPI_COMM_WORLD);
}

/* Print the result */
if (my_rank == 0) {
    printf("With n = %d trapezoids, our estimate\n",
           n);
    printf("of the integral from %f to %f = %f\n",
           a, b, total);
}

/* Shut down MPI */
MPI_Finalize();
} /* main */
```

Home work 😊

- Vector maximum
- Search of an element in a vector
- Summation of two matrixes
- From Pacheco, Programming Assignment 3.7.1
- From Pacheco, Exercise 4.6.2, Programming Assignment 4.7.1, 4.7.2

Hard Homework ☹️

- Matrix – Matrix Product ($AxB=C$)
- Advice:

```
for (each column x of B) {  
    Compute parallel dot product matrix-  
    vettor Ax  
}
```



```

#include <mpi.h>
#include <stdio.h>

#define MAXSIZE 100000

int main(int argc, char** argv)
{
    int myid, numprocs;
    int x, low, high, result_temp, i;
    int dest, source;
    int *data, *local_data;
    double myresult, result;
    double start, end;
    MPI_Status status;
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD, &myid);

    result = 0;
    myresult = 0;
    // Inizializzo...(ogni "processo" vedrà la propria porzione inizializzata)
    if (myid==0){
        data = new int[MAXSIZE];
        for (i=0; i<MAXSIZE;i++)
            data[i] = i;
    }
    start = MPI_Wtime();
    // Individuo la mia porzione
    x = MAXSIZE/numprocs;
    local_data = new int[x];
    MPI_Scatter(data, x, MPI_INT, local_data, x, MPI_INT, 0, MPI_COMM_WORLD);

    // Calcolo il mio risultato (anche il processo 0 lo farà)
    for (i=0; i<x; i++)
        myresult = myresult + local_data[i];
    if (myid == 0){
        result = myresult;
        for (source=1; source<numprocs; source++){
            MPI_Recv(&myresult, 1, MPI_DOUBLE, source, 0, MPI_COMM_WORLD, &status);
            result = result + myresult;
        }
    }
    else
        MPI_Send(&myresult, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD);

    end = MPI_Wtime();
    if (myid == 0){
        printf("La somma è %e.\n", result);
        printf("Calcolato in tempo %f milliseccs\n", 1000*(end - start));
    }
    MPI_Finalize();
}

```

Sum of the elements of a vector (dynamic allocation)

Compile with mpiCC!

Scalar Product

Let

$$x = (x_0, x_1, \dots, x_{n-1})^T$$

$$y = (y_0, y_1, \dots, y_{n-1})^T$$

$$x \oplus y = x_0y_0 + x_1y_1 + \dots + x_{n-1}y_{n-1}$$

Serial

```
#include <stdio.h>

#define MAX_ORDER 100

main() {
    float  x[MAX_ORDER];
    float  y[MAX_ORDER];
    int    n;
    float  dot;

    void Read_vector(char* prompt, float v[], int n);
    float Serial_dot(float x[], float y[], int n);

    printf("Enter the order of the vectors\n");
    scanf("%d", &n);
    Read_vector("the first vector", x, n);
    Read_vector("the second vector", y, n);
    dot = Serial_dot(x, y, n);
    printf("The dot product is %f\n", dot);
} /* main */
```

```
/******
void Read_vector(
    char*  prompt /* in */,
    float  v[]    /* out */,
    int    n      /* in */) {
    int i;

    printf("Enter %s\n", prompt);
    for (i = 0; i < n; i++)
        scanf("%f", &v[i]);
} /* Read_vector */

/******
float Serial_dot(
    float  x[] /* in */,
    float  y[] /* in */,
    int    n  /* in */) {
    int    i;
    float  sum = 0.0;

    for (i = 0; i < n; i++)
        sum = sum + x[i]*y[i];
    return sum;
} /* Serial_dot */
```

Parallel – Block Mapping

<i>Process</i>	<i>Components</i>
0	$x_0, x_1, \dots, x_{\check{n}-1}$
1	$x_{\check{n}}, x_{\check{n}+1}, \dots, x_{2\check{n}-1}$
.	.
.	.
k	$x_{k\check{n}}, x_{k\check{n}+1}, \dots, x_{(k+1)\check{n}-1}$
.	.
.	.
$p-1$	$x_{(p-1)\check{n}}, x_{(p-1)\check{n}+1}, \dots, x_{n-1}$

Parallel – Block Mapping

- This allocation "technique" is different than that used, for example, for the "sum of the elements of a vector", where each process sees the entire data structure
- In this case, although each process **allocates the entire data structure**, it receives only the portion of data that interests it

Parallel

```
#include <stdio.h>
#include "mpi.h"

#define MAX_LOCAL_ORDER 100

main(int argc, char* argv[]) {
    float local_x[MAX_LOCAL_ORDER];
    float local_y[MAX_LOCAL_ORDER];
    int n;
    int n_bar; /* = n/p */
    float dot;
    int p;
    int my_rank;

    void Read_vector(char* prompt, float local_v[], int n_bar, int p,
                    int my_rank);
    float Parallel_dot(float local_x[], float local_y[], int n_bar);

    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &p);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    if (my_rank == 0) {
        printf("Enter the order of the vectors\n");
        scanf("%d", &n);
    }
    MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
    n_bar = n/p;

    Read_vector("the first vector", local_x, n_bar, p, my_rank);
    Read_vector("the second vector", local_y, n_bar, p, my_rank);

    dot = Parallel_dot(local_x, local_y, n_bar);

    if (my_rank == 0)
        printf("The dot product is %f\n", dot);

    MPI_Finalize();
} /* main */
```

“broadcast” n to all!



Vector portion \bar{n}



Broadcast more efficient than multiple sends!

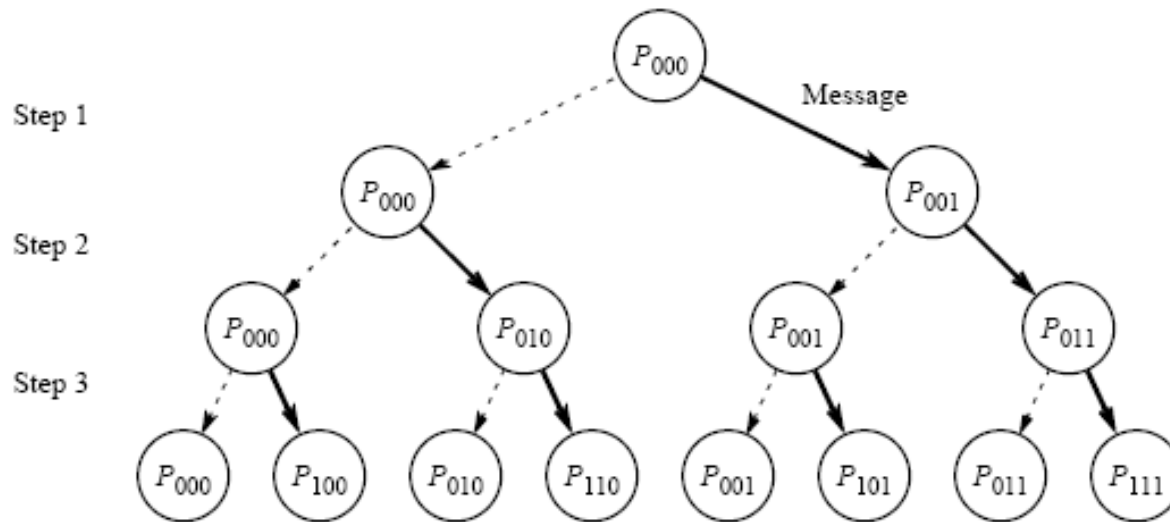


Figure 2.21 Broadcast as a tree construction.

OSS: A Reduce in practice does the reverse path, so both have $O(\log n)$ cost

Block mapping

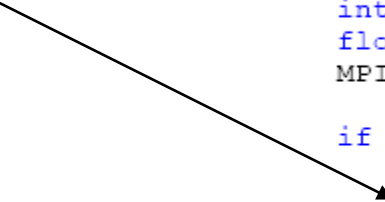
```

/*****
void Read_vector(
    char*  prompt    /* in  */,
    float  local_v[] /* out */,
    int    n_bar     /* in  */,
    int    p         /* in  */,
    int    my_rank   /* in  */) {
    int i, q;
    float temp[MAX_LOCAL_ORDER];
    MPI_Status status;


    if (my_rank == 0) {
        printf("Enter %s\n", prompt);
        for (i = 0; i < n_bar; i++)
            scanf("%f", &local_v[i]);
        for (q = 1; q < p; q++) {
            for (i = 0; i < n_bar; i++)
                scanf("%f", &temp[i]);
            MPI_Send(temp, n_bar, MPI_FLOAT, q, 0, MPI_COMM_WORLD);
        }
    } else {
        MPI_Recv(local_v, n_bar, MPI_FLOAT, 0, 0, MPI_COMM_WORLD,
                &status);
    }
} /* Read_vector */

```

Read portion for process 0




Reads n elements and sends them (Block mapping) one Process at a time



NB Use Scatter (homework)

Only the first n_bar of `local_v` are what each process needs!




```

/*****
float Serial_dot(
    float  x[]  /* in */,
    float  y[]  /* in */,
    int    n    /* in */) {

    int    i;
    float  sum = 0.0;

    for (i = 0; i < n; i++)
        sum = sum + x[i]*y[i];
    return sum;
} /* Serial_dot */

```

```

/*****
float Parallel_dot(
    float  local_x[] /* in */,
    float  local_y[] /* in */,
    int    n_bar     /* in */) {

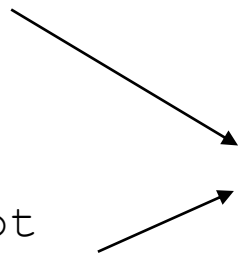
    float  local_dot;
    float  dot = 0.0;
    float  Serial_dot(float x[], float y[], int m);

    local_dot = Serial_dot(local_x, local_y, n_bar);
    MPI_Reduce(&local_dot, &dot, 1, MPI_FLOAT,
              MPI_SUM, 0, MPI_COMM_WORLD);
    return dot;
} /* Parallel_dot */

```

Each process has allocated all the vector, but only the first \bar{n} elements are its

reduce.... Do the sum of all local_dot and place in dot



Matrix-Vector Product

Let $A=(a_{ij})$ be a $m \times n$ matrix

Let $x=(x_0, x_1, \dots, x_{n-1})^T$

The **product** $y = Ax$, is formed by all scalar products of each row of A with x

Thus, the vector y will be given by:

$$y=(y_0, y_1, \dots, y_{m-1})^T$$

with:

$$y_k = a_{k0}x_0 + a_{k1}x_1 + \dots + a_{k,n-1}x_{n-1}$$

Serial

```

/*****
void Serial_matrix_vector_prod(
    MATRIX_T A /* in */,
    int m /* in */,
    int n /* in */,
    float x[] /* in */,
    float y[] /* out */) {

    int k, j;

    for (k = 0; k < m; k++) {
        y[k] = 0.0;

        for (j = 0; j < n; j++)
            y[k] = y[k] + A[k][j]*x[j];
    }
} /* Serial_matrix_vector_prod */

```

Data Distribution

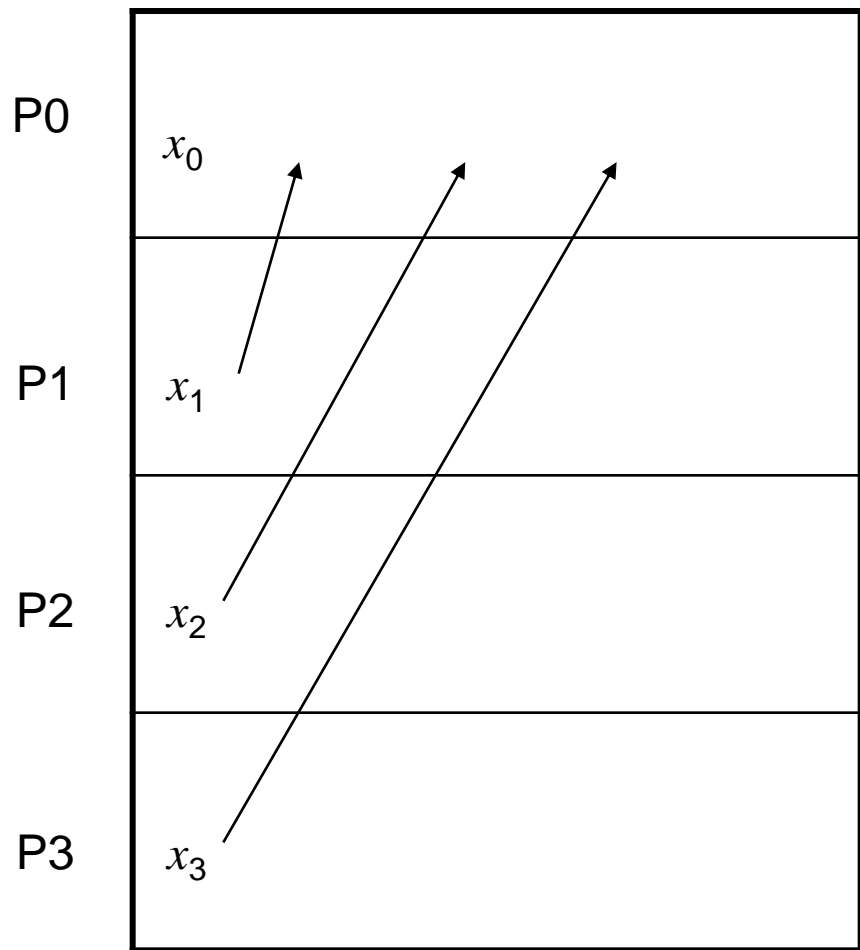
- Block-row (panel) distribution

Process	Elements			
0	a_{00}	a_{01}	a_{02}	a_{03}
	a_{10}	a_{11}	a_{12}	a_{13}
1	a_{20}	a_{21}	a_{22}	a_{23}
	a_{30}	a_{31}	a_{32}	a_{33}
2	a_{40}	a_{41}	a_{42}	a_{43}
	a_{50}	a_{51}	a_{52}	a_{53}
3	a_{60}	a_{61}	a_{62}	a_{63}
	a_{70}	a_{71}	a_{72}	a_{73}

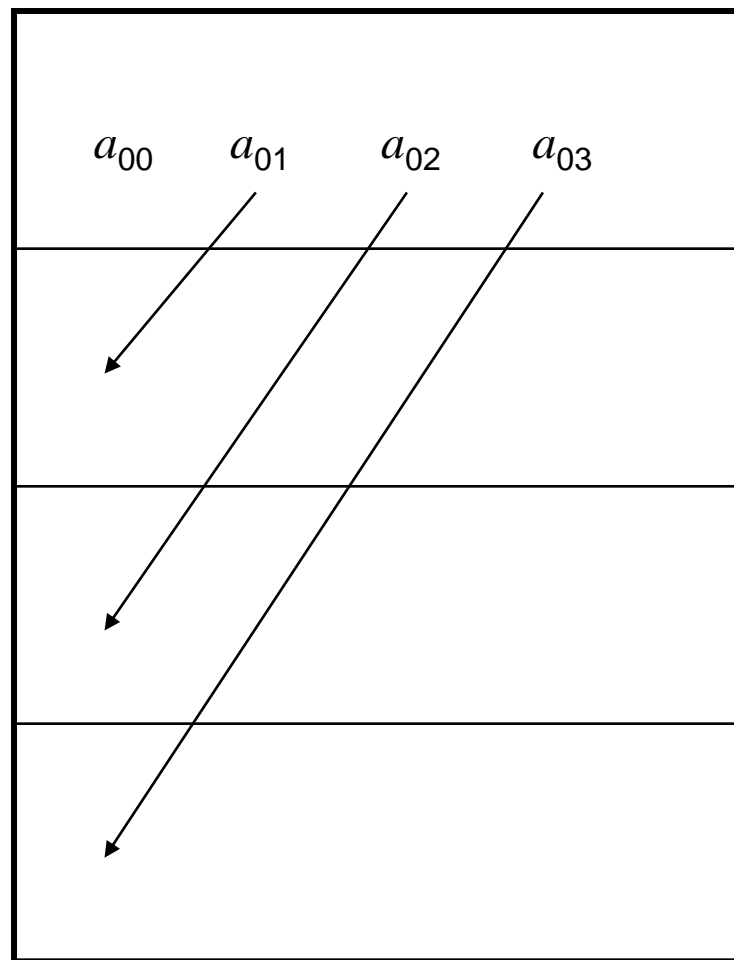
Gather or scatter?

- In order to form the scalar product of each row of A with x , we must make a **gather** of x on each process, or a **scatter** of each row of A on the processes
- For example, if $m = n = p = 4$, then $a_{00}, a_{01}, a_{02}, a_{03}$ and x_0 are assigned to process 0, x_1 to process 1, x_2 to process 2, etc..
- In this way, to form the scalar product of the first row of A with x , we can
 - send x_1, x_2 and x_3 to the process 0, **or**
 - we can send a_{01} to the process 1, a_{02} to process 2 and a_{03} to process 3.
- The first step is a **gather**, the second a **scatter**!
- We will use gather in the example below ... (scatter for the reading stage!)

$$m=n=p=4$$



Gather



Scatter

```

#include <stdio.h>
#include "mpi.h"

#define MAX_ORDER 100

typedef float LOCAL_MATRIX_T[MAX_ORDER][MAX_ORDER];

main(int argc, char* argv[]) {
    int my_rank;
    int p;
    LOCAL_MATRIX_T local_A;
    float global_x[MAX_ORDER];
    float local_x[MAX_ORDER];
    float local_y[MAX_ORDER];
    int m, n;
    int local_m, local_n;

    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &p);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    if (my_rank == 0) {
        printf("Enter the order of the matrix (m x n)\n");
        scanf("%d %d", &m, &n);
    }
    MPI_Bcast(&m, 1, MPI_INT, 0, MPI_COMM_WORLD);
    MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);

    local_m = m/p;
    local_n = n/p;

    Read_matrix("Enter the matrix", local_A, local_m, n, my_rank, p);
    Print_matrix("We read", local_A, local_m, n, my_rank, p);

    Read_vector("Enter the vector", local_x, local_n, my_rank, p);
    Print_vector("We read", local_x, local_n, my_rank, p);

    Parallel_matrix_vector_prod(local_A, m, n, local_x, global_x,
        local_y, local_m, local_n);
    Print_vector("The product is", local_y, local_m, my_rank, p);

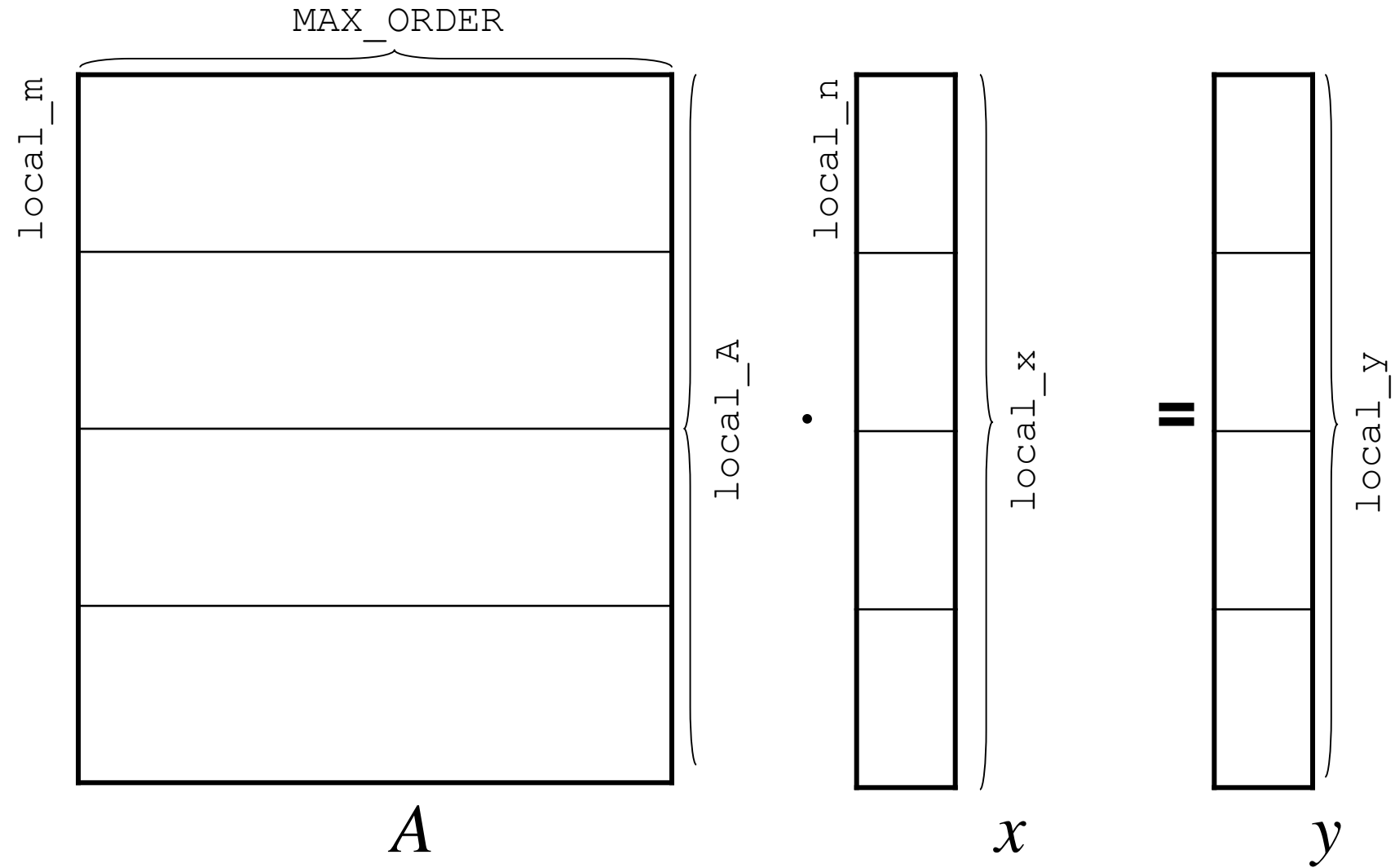
    MPI_Finalize();

} /* main */

```

main

Mapping



Read and data allocation

```
/******  
void Read_matrix(  
    char*      prompt /* in */,  
    LOCAL_MATRIX_T local_A /* out */,  
    int        local_m /* in */,  
  
    int        n /* in */,  
    int        my_rank /* in */,  
    int        p /* in */) {  
  
    int        i, j;  
    LOCAL_MATRIX_T temp;  
  
    /* Fill dummy entries in temp with zeroes */  
    for (i = 0; i < p*local_m; i++)  
        for (j = n; j < MAX_ORDER; j++)  
            temp[i][j] = 0.0;  
  
    if (my_rank == 0) {  
        printf("%s\n", prompt);  
        for (i = 0; i < p*local_m; i++)  
            for (j = 0; j < n; j++)  
                scanf("%f", &temp[i][j]);  
    }  
    MPI_Scatter(temp, local_m*MAX_ORDER, MPI_FLOAT, local_A,  
                local_m*MAX_ORDER, MPI_FLOAT, 0, MPI_COMM_WORLD);  
} /* Read_matrix */
```

Sets to zero the surplus elements of the matrix

Process 0: reads all the matrix

Process 0: scatter all matrix, but each process will receive only local_A (in C le matrici sono row-wise)

CAREFUL! Scatter ok for static allocated matrix/vectors!

Read and data allocation

```

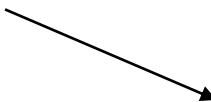
/*****
void Read_vector(
    char*  prompt    /* in */,
    float  local_x[] /* out */,
    int    local_n   /* in */,
    int    my_rank   /* in */,
    int    p         /* in */) {

    int    i;
    float  temp[MAX_ORDER];

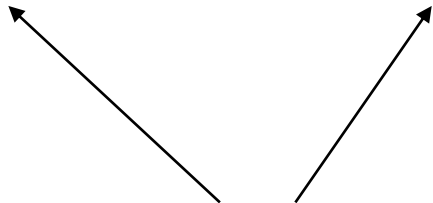
    if (my_rank == 0) {
        printf("%s\n", prompt);
        for (i = 0; i < p*local_n; i++)
            scanf("%f", &temp[i]);
    }
    MPI_Scatter(temp, local_n, MPI_FLOAT, local_x, local_n, MPI_FLOAT,
               0, MPI_COMM_WORLD);
} /* Read_vector */

```

Reads all the vector and
scatters it!



NB Like in all Scatters, it
should be the same!



AllGather

```
void Parallel_matrix_vector_prod(
    LOCAL_MATRIX_T local_A    /* in */,
    int             m         /* in */,
    int             n         /* in */,
    float          local_x[]  /* in */,
    float          global_x[] /* in */,
    float          local_y[]  /* out */,
    int            local_m    /* in */,
    int            local_n    /* in */) {

    /* local_m = m/p, local_n = n/p */

    int i, j;

    MPI_Allgather(local_x, local_n, MPI_FLOAT,
                 global_x, local_n, MPI_FLOAT,
                 MPI_COMM_WORLD);
    for (i = 0; i < local_m; i++) {
        local_y[i] = 0.0;
        for (j = 0; j < n; j++)
            local_y[i] = local_y[i] +
                local_A[i][j]*global_x[j];
    }
} /* Parallel_matrix_vector_prod */
```

“We collect the pieces of x
on each process (in global_x)

WE could of used also
MPI_Gather with a for on all
processes

Matrix – Matrix Product : Serial Algorithm

- $O(n^3)$ Cost

```
1.  procedure MAT_MULT (A, B, C)
2.  begin
3.      for i := 0 to n - 1 do
4.          for j := 0 to n - 1 do
5.              begin
6.                  C[i, j] := 0;
7.                  for k := 0 to n - 1 do
8.                      C[i, j] := C[i, j] + A[i, k] × B[k, j];
9.                  endfor;
10. end MAT_MULT
```

Algorithm 8.2 The conventional serial algorithm for multiplication of two $n \times n$ matrices.

Matrix – Matrix Product : Possible Allocations

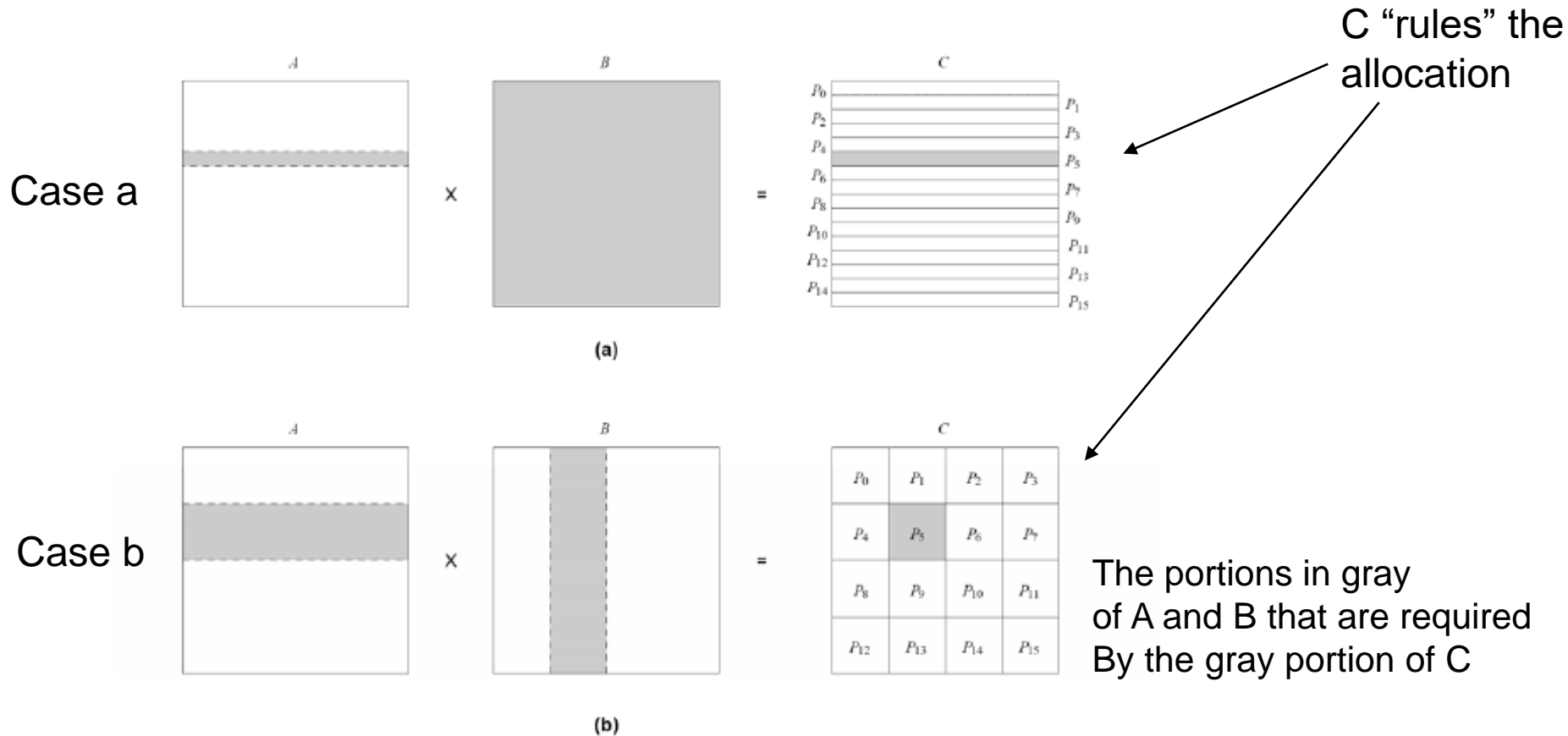


Figure 3.26 Data sharing needed for matrix multiplication with (a) one-dimensional and (b) two-dimensional partitioning of the output matrix. Shaded portions of the input matrices A and B are required by the process that computes the shaded portion of the output matrix C .

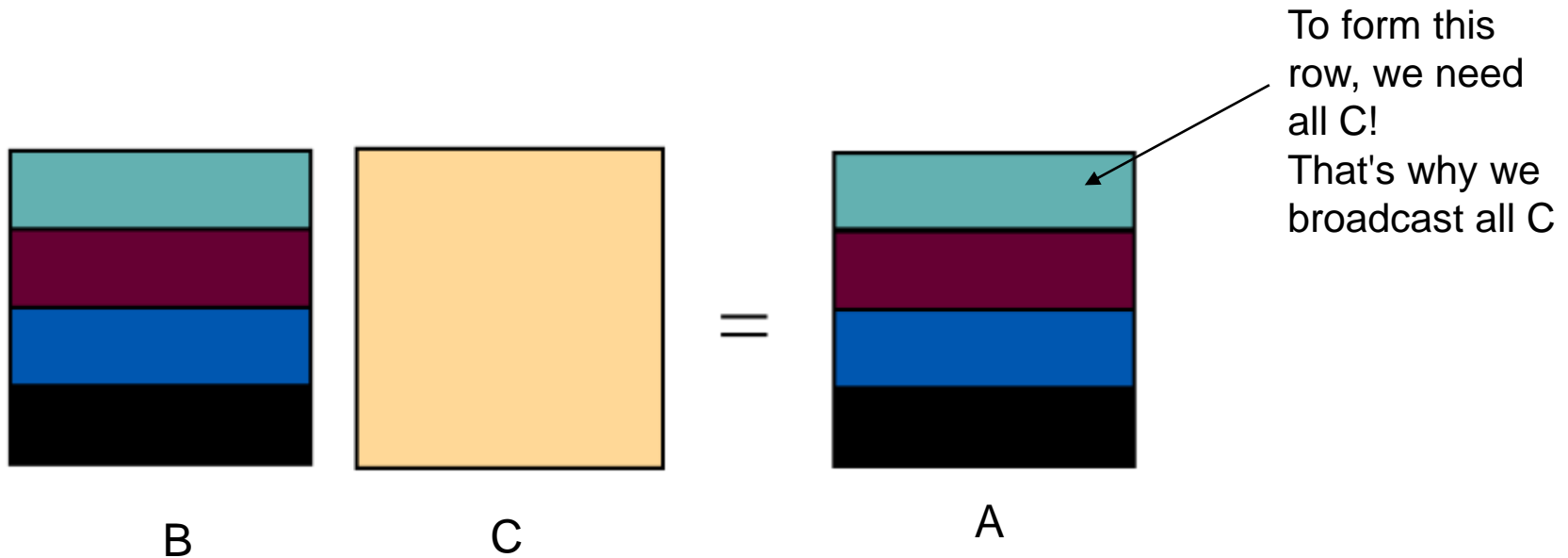
Matrix – Matrix Product

- For simplicity, we consider matrices of the same order (n, n)
- In case (a) we have a decomposition into one-dimensional blocks ; in (b) a bi-dimensional block decomposition
- Each process in the case (a) will have n / p rows, while in case (b), each process will have a block of dim

$$n / \sqrt{p} \times n / \sqrt{p}$$

- In (a) we can use up to n processes, in (b) up to n^2 (thus increasing the degree of parallelism)
- The "counter" of case (a) is that each process requires the corresponding n / p rows of A and of the whole B matrix, while in (b) each process requires n / \sqrt{p} rows of A and n / \sqrt{p} columns of B

Algorithm case (a)



- **Distribute the rows of B to all** (Scatter)
- **Broadcast** all C (unfortunately !)
- Form the product of C with rows of B for each process.
These will be the corresponding rows of A
- Returns the rows of A to a process using a **gather**
- This algorithm is different from that suggested by Pacheco, but similar to that of the LLNL tutorial (master / slave)


```
#include <stdio.h>
#include <mpi.h>
```

```
#define NCOLS 4
#define NROWS 4
```

The algorithm applies only to these values! Generalize it!

Algorithm case (a)

```
int main(int argc, char **argv) {
```

```
    int i,j,k,l;
```

```
    int ierr, rank, size, root;
```

```
    float A[NROWS][NCOLS];
```

```
    float Apart[NCOLS];
```

```
    float Bpart[NCOLS];
```

```
    float C[NROWS][NCOLS];
```

```
    float B̄[NCOLS][NCOLS];
```

```
    root = 0;
```

```
    ....
```

```
    /* Scatter matrix B by rows. */
```

```
    ierr=MPI_Scatter(B,NCOLS,MPI_FLOAT,Bpart,NCOLS,MPI_FLOAT,root,MPI_COMM_WORLD);
```

```
    /* Broadcast C */
```

```
    ierr=MPI_Bcast(C,NROWS*NCOLS,MPI_FLOAT,root,MPI_COMM_WORLD);
```

```
    /* Do the vector-scalar multiplication. */
```

```
    for(j=0;j<NCOLS;j++){
```

```
        Apart[j] = 0.0;
```

```
        for(k=0; k<NROWS; k++)
```

```
            Apart[j] += Bpart[k]*C[k][j];
```

```
    }
```

```
    ....
```

```
    /* Gather matrix A. */
```

```
    ierr=MPI_Gather(Apart,NCOLS,MPI_FLOAT,A,NCOLS,MPI_FLOAT,root,MPI_COMM_WORLD);
```

```
    /* Report results */
```

```
    if (rank == 0) {
```

```
        printf("\nThis is the result of the parallel computation:\n\n");
```

```
        for(j=0;j<NROWS;j++) {
```

```
            for(k=0;k<NCOLS;k++) {
```

```
                printf("A[%d][%d]=%g\n",j,k,A[j][k]);
```

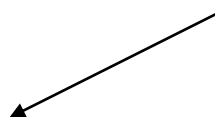
```
            }
```

```
        }
```

$A=B \times C$

The algorithm applies to only
4 processors!
Generalize it!

Remember what a gather does!
A is constructed from many Apart pieces!
That is, we collect the various rows!



Algorithm case (b)

- Suppose, for example, the partitioning of data as in Fig.
- The 4 submatrixes $C_{i,j}$ (of dimension $n/2 \times n/2$), can be computed independently

$$\begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \cdot \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix} \rightarrow \begin{pmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{pmatrix}$$

(a)

$$\text{Task 1: } C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1}$$

$$\text{Task 2: } C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2}$$

$$\text{Task 3: } C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1}$$

$$\text{Task 4: } C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2}$$

(b)

OBS: other partitionings are also possible!

Block Algorithm (Serial) – Case (b)

```
1.  procedure BLOCK_MAT_MULT ( $A, B, C$ )
2.  begin
3.      for  $i := 0$  to  $q - 1$  do
4.          for  $j := 0$  to  $q - 1$  do
5.              begin
6.                  Initialize all elements of  $C_{i,j}$  to zero;
7.                  for  $k := 0$  to  $q - 1$  do
8.                       $C_{i,j} := C_{i,j} + A_{i,k} \times B_{k,j}$ ; ← Product and sum of matrixes
9.                  endfor;
10. end BLOCK_MAT_MULT
```

Algorithm 8.3 The block matrix multiplication algorithm for $n \times n$ matrices with a block size of $(n/q) \times (n/q)$.

Parallel Algorithm (case b)

- Consider two matrixes $(n \times n)$ A e B partitioned in p blocks $A_{i,j}$ and $B_{i,j}$ ($0 \leq i, j < \sqrt{p}$) di dimension n
- Initially process $P_{i,j}$ stores $A_{i,j}$ and $B_{i,j}$ and computes the block $C_{i,j}$ of the resulting matrix $(n/\sqrt{p}) \times (n/\sqrt{p})$
- The computation of the submatrix $C_{i,j}$ requires all submatrixes $A_{i,k}$ and $B_{k,j}$ for $0 \leq k < \sqrt{p}$
- Execute All-to-all broadcast (that is `MPI_Allgather`) of A blocks along the rows and of B along columns
- Execute the multiplication of local submatrixes
- **Obs:** The cost of this algorithm is identical to the serial version (n^3) : q^3 matrix products are carried out, each of $(n/q) \times (n/q)$ matrixes and $(n/q)^3$ additions and multiplications

Homework 😊 - again?

- Pi computation with Montecarlo
- Vector Maximum
- Search of element in a vector
- Sum of two matrixes

```

#include <mpi.h>
#include <stdio.h>

#define MAXSIZE 10

int main(int argc, char** argv)
{
    int myid, numprocs;
    int data[MAXSIZE], i, x, low, high, myresult, result;
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD, &myid);

    result = 0;
    myresult = 0;

    if (myid == 0)
    {
        // Inizializzo...
        for (i=0; i<MAXSIZE;i++)
            data[i] = i;
    }

    // Invio il vettore
    MPI_Bcast(data, MAXSIZE, MPI_INT, 0, MPI_COMM_WORLD);

    // NB Tutti i processi (compresi 0) calcolano...
    x = MAXSIZE/numprocs;
    low = myid * x;
    high = low + x;
    for (i=low; i<high; i++)
        myresult = myresult + data[i];

    printf("Il processo %d ha calcolato %d\n", myid, myresult);

    MPI_Reduce(&myresult, &result, 1, MPI_INT, MPI_SUM, 0, MPI_COMM_WORLD);
    if (myid ==0)
        printf("La somma è %d.\n", result);

    MPI_Finalize();
    exit(0);
}

```

Sum of elements of a vector

Not memory optimal!
Look following slide!



```

#include <mpi.h>
#include <stdio.h>

#define MAXSIZE 100000

int main(int argc, char** argv)
{
    int myid, numprocs;
    int x, low, high, result_temp, i;
    int dest, source;
    int *data, *local_data;
    double myresult, result;
    double start, end;
    MPI_Status status;
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD, &myid);

    result = 0;
    myresult = 0;
    // Inizializzo...(ogni "processo" vedrà la propria porzione inizializzata)
    if (myid==0){
        data = new int[MAXSIZE];
        for (i=0; i<MAXSIZE;i++)
            data[i] = i;
    }
    start = MPI_Wtime();
    // Individuo la mia porzione
    x = MAXSIZE/numprocs;
    local_data = new int[x];
    MPI_Scatter(data, x, MPI_INT, local_data, x, MPI_INT, 0, MPI_COMM_WORLD);

    // Calcolo il mio risultato (anche il processo 0 lo farà)
    for (i=0; i<x; i++)
        myresult = myresult + local_data[i];
    if (myid == 0){
        result = myresult;
        for (source=1; source<numprocs; source++){
            MPI_Recv(&myresult, 1, MPI_DOUBLE, source, 0, MPI_COMM_WORLD, &status);
            result = result + myresult;
        }
    }
    else
        MPI_Send(&myresult, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD);

    end = MPI_Wtime();
    if (myid == 0){
        printf("La somma è %e.\n", result);
        printf("Calcolato in tempo %f milliseccs\n", 1000*(end - start));
    }
    MPI_Finalize();
}

```

**Sum of elements o a
vector (dynamic
allocation)**

Compile with mpiCC !

Matrix Scatter

```
#include "mpi.h"
#include <stdio.h>
#define SIZE 4

int main(argc,argv)
int argc;
char *argv[]; {
int numtasks, rank, sendcount, recvcount, source;
float sendbuf[SIZE][SIZE] = {
    {1.0, 2.0, 3.0, 4.0},
    {5.0, 6.0, 7.0, 8.0},
    {9.0, 10.0, 11.0, 12.0},
    {13.0, 14.0, 15.0, 16.0} };
float recvbuf[SIZE];

MPI_Init(&argc,&argv);
MPI_Comm_rank(MPI_COMM_WORLD, &rank);
MPI_Comm_size(MPI_COMM_WORLD, &numtasks);

if (numtasks == SIZE) {
    source = 1;
    sendcount = SIZE;
    recvcount = SIZE;
    MPI_Scatter(sendbuf,sendcount,MPI_FLOAT,recvbuf,recvcount,
               MPI_FLOAT,source,MPI_COMM_WORLD);

    printf("rank= %d Results: %f %f %f %f\n",rank,recvbuf[0],
           recvbuf[1],recvbuf[2],recvbuf[3]);
}
else
    printf("Must specify %d processors. Terminating.\n",SIZE);

MPI_Finalize();
}
```

NB Scatter called by all processes!

Output

```
{
rank= 0 Results: 1.000000 2.000000 3.000000 4.000000
rank= 1 Results: 5.000000 6.000000 7.000000 8.000000
rank= 2 Results: 9.000000 10.000000 11.000000 12.000000
rank= 3 Results: 13.000000 14.000000 15.000000 16.000000
}
```


Get_data2 (with Broadcast)

```
/* **** */
/* Function Get_data2
 * Reads in the user input a, b, and n.
 * Input parameters:
 * 1. int my_rank: rank of current process.
 * 2. int p: number of processes.
 * Output parameters:
 * 1. float* a_ptr: pointer to left endpoint a.
 * 2. float* b_ptr: pointer to right endpoint b.
 * 3. int* n_ptr: pointer to number of trapezoids.
 * Algorithm:
 * 1. Process 0 prompts user for input and
 *    reads in the values.
 * 2. Process 0 sends input values to other
 *    processes using three calls to MPI_Bcast.
 */
void Get_data2(
    float* a_ptr /* out */,
    float* b_ptr /* out */,
    int* n_ptr /* out */,
    int my_rank /* in */) {

    if (my_rank == 0) {
        printf("Enter a, b, and n\n");
        scanf("%f %f %d", a_ptr, b_ptr, n_ptr);
    }
    MPI_Bcast(a_ptr, 1, MPI_FLOAT, 0, MPI_COMM_WORLD);
    MPI_Bcast(b_ptr, 1, MPI_FLOAT, 0, MPI_COMM_WORLD);
    MPI_Bcast(n_ptr, 1, MPI_INT, 0, MPI_COMM_WORLD);
} /* Get_data2 */
```

```
#include <stdio.h>

/* We'll be using MPI routines, definitions, etc. */
#include "mpi.h"

main(int argc, char** argv) {

    ....

    MPI_Init(&argc, &argv);

    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    MPI_Comm_size(MPI_COMM_WORLD, &p);

    Get_data2(&a, &b, &n, my_rank); ← Get_data2!

    h = (b-a)/n;    /* h is the same for all processes */
    local_n = n/p; /* So is the number of trapezoids */

    /* Length of each process' interval of
     * integration = local_n*h.  So my interval
     * starts at: */
    local_a = a + my_rank*local_n*h;
    local_b = local_a + local_n*h;
    integral = Trap(local_a, local_b, local_n, h);

    /* Add up the integrals calculated by each process */
    MPI_Reduce(&integral, &total, 1, MPI_FLOAT,
              MPI_SUM, 0, MPI_COMM_WORLD);

    /* Print the result */
    if (my_rank == 0) {
        printf("With n = %d trapezoids, our estimate\n",
              n);
        printf("of the integral from %f to %f = %f\n",
              a, b, total);
    }

    /* Shut down MPI */
    MPI_Finalize();
} /* main */
```

Numerical integration (final)

```
...
MPI_Barrier(MPI_COMM_WORLD);
start = MPI_Wtime();

h = (b-a)/n;    /* h is the same for all processes */
local_n = n/p; /* So is the number of trapezoidals */

/* Length of each process' interval of
 * integration = local_n*h. So my interval
 * starts at: */
local_a = a + my_rank*local_n*h;
local_b = local_a + local_n*h;

/* Call the serial trapezoidal function */
integral = Trap(local_a, local_b, local_n, h);

/* Add up the integrals calculated by each process */
MPI_Reduce(&integral, &total, 1, MPI_FLOAT,
          MPI_SUM, 0, MPI_COMM_WORLD);

MPI_Barrier(MPI_COMM_WORLD);
finish = MPI_Wtime();
/* Print the result */
if (my_rank == 0) {
    printf("With n = %d trapezoids, our estimate\n",
           n);
    printf("of the integral from %f to %f = %f\n",
           a, b, total);
    printf("Elapsed time in seconds", "%e",
           (finish - start) - overhead);
}

MPI_Finalize();
} /* main */
```

?



Wow!

```
*/
#include <stdio.h>
#include "mpi.h"
#include "cio.h"

main(int argc, char* argv[]) {
    ...
    MPI_Comm io_comm;
    ...

    float Trap(float local_a, float local_b, int local_n,
               float h); /* Calculate local integral */

    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &p);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
    MPI_Comm_dup(MPI_COMM_WORLD, &io_comm);
    Cache_io_rank(MPI_COMM_WORLD, io_comm);

    Cscanf(io_comm, "Enter a, b, and n", "%f %f %d", &a, &b, &n);

    /* Estimate overhead */
    overhead = 0.0;
    for (i = 0; i < 100; i++) {
        MPI_Barrier(MPI_COMM_WORLD);
        start = MPI_Wtime();
        MPI_Barrier(MPI_COMM_WORLD);
        finish = MPI_Wtime();
        overhead = overhead + (finish - start);
    }
    overhead = overhead/100.0;

    MPI_Barrier(MPI_COMM_WORLD);
    start = MPI_Wtime();

    h = (b-a)/n; /* h is the same for all processes */
    local_n = n/p; /* So is the number of trapezoidals */

    /* Length of each process' interval of
     * integration = local_n*h. So my interval
     * starts at: */
    local_a = a + my_rank*local_n*h;
    local_b = local_a + local_n*h;

    /* Call the serial trapezoidal function */
    integral = Trap(local_a, local_b, local_n, h);

    /* Add up the integrals calculated by each process */
    MPI_Reduce(&integral, &total, 1, MPI_FLOAT,
              MPI_SUM, 0, MPI_COMM_WORLD);

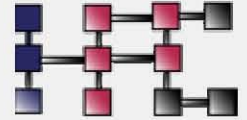
    MPI_Barrier(MPI_COMM_WORLD);
    finish = MPI_Wtime();
    Cprintf(io_comm, "Our estimate is", "%f", total);
    Cprintf(io_comm, "Elapsed time in seconds", "%e",
            (finish - start) - overhead);

    MPI_Finalize();
} /* main */
```

Barrier estimation time
(average on 100 times)

Calcolo di π :

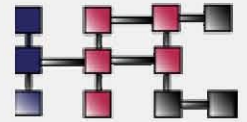
un esempio



- Calcoliamo π tramite integrazione numerica
- Usando le seguenti routine MPI:
MPI_BARRIER, MPI_BCAST, MPI_REDUCE

$$\pi = \int_0^1 \frac{4}{1+x^2} dx$$

Pseudocodice seriale

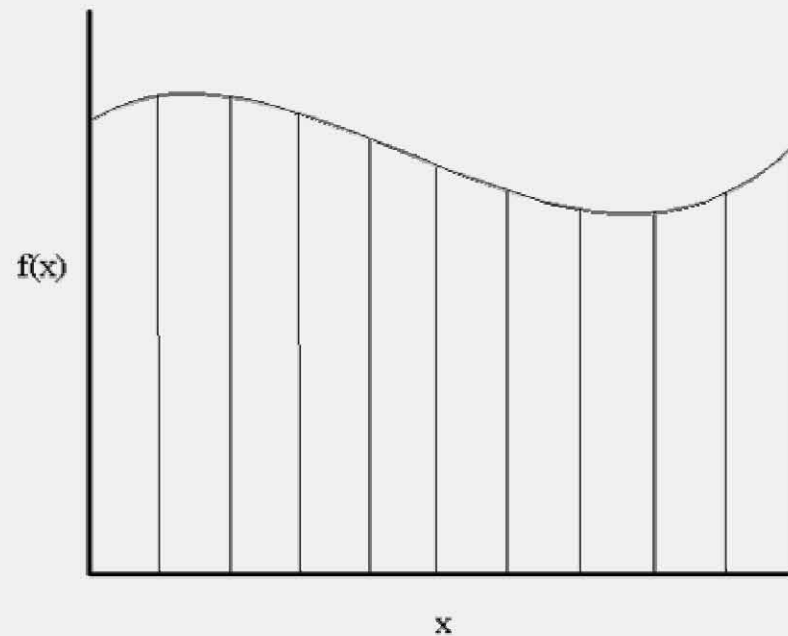


```
f(x) = 1/(1+x2)
h = 1/N, sum = 0.0
do i = 1, N
    x = h*(i - 0.5)
    sum = sum + f(x)
enddo
pi = h * sum
```

Esempio:

$N = 10, h=0.1$

$x = \{.05, .15, .25, .35, .45,$
 $.55, .65, .75, .85, .95\}$



Pseudocodice parallelo

P(0) legge N e lo spedisce con broadcast a tutti i processori

$$f(x) = 1/(1+x^2)$$

$$h = 1/N, \text{ sum} = 0.0$$

do i = **my_rank**+1, N, **nproc**

$$x = h*(i - 0.5)$$

$$\text{sum} = \text{sum} + f(x)$$

enddo

$$\text{mypi} = h * \text{sum}$$

P(0) colleziona la variabile mypi da ogni processore e la riduce al valore pi

Esempio:

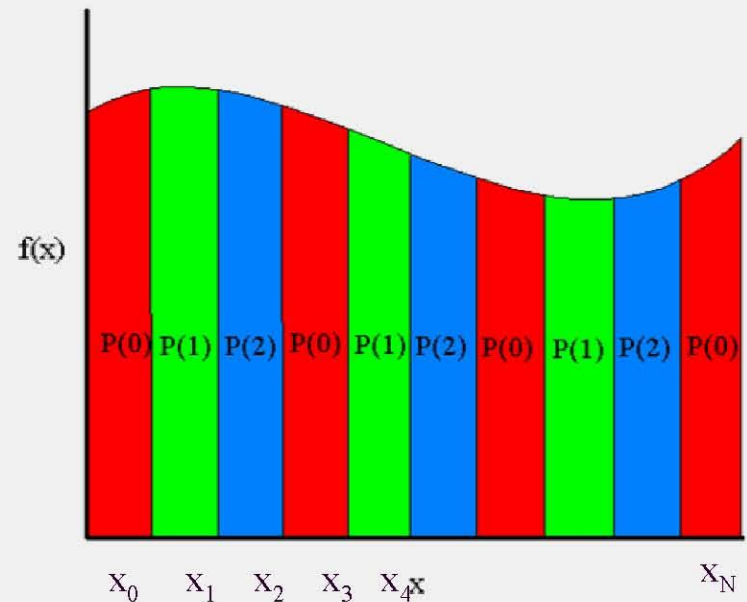
$$N = 10, h=0.1$$

Procrs: {P(0),P(1),P(2)}

P(0) -> {.05, .35, .65, .95}

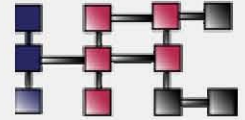
P(1) -> {.15, .45, .75}

P(2) -> {.25, .55, .85}



Calcolo di π :

il programma

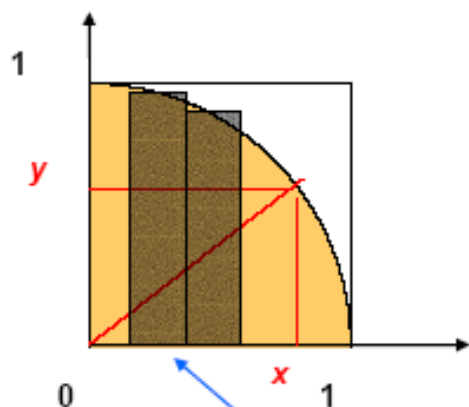


```
int n; /* Numero di rettangoli */
int nproc, myrank;
MPI_Init(&argc,&argv);
MPI_Comm_rank(MPI_COMM_WORLD,&my_rank);
MPI_Comm_Size(MPI_COMM_WORLD,&nproc);
if (my_rank == 0) read_from_keyboard(&n);

MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
h = 1.0 / (double) n;
  sum = 0.0;
  for (i = my_rank + 1; i <= n; i += nproc) {
    x = h * ((double)i - 0.5);
    sum += 4.0 / (1.0 + x*x);
  }
  mypi = h * sum;

MPI_Reduce(&mypi, &pi, 1, MPI_DOUBLE, MPI_SUM, 0,
MPI_COMM_WORLD);
```


Calcolo PI greco



E' noto che l'area del cerchio è $r^2 \pi$, per cui l'area del semicerchio con $r=1$ è:

$$\pi/4$$

Curva cerchio (teorema di Pitagora):

$$x^2 + y^2 = 1$$

$$y = \sqrt{1-x^2}$$

L'area del semicerchio corrisponde al calcolo del seguente integrale:

$$\int_0^1 \sqrt{1-X^2}$$

Equivalentemente
possiamo calcolare

$$\int_0^1 \frac{1}{1+x^2}$$

$$\text{ARCTAN}(1) = \pi/4$$

$$\text{ARCTAN}(0) = 0$$

Possiamo calcolarlo numericamente. Maggiore è il numero di intervalli in cui suddividiamo $[0..1]$, maggiore è la precisione del calcolo dell'integrale

Esempio: PI greco in C (1)

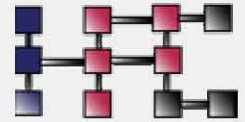
```
#include <mpi.h>
#include <math.h>

int main(int argc, char *argv[])
{
    int done = 0, n, myid, numprocs, i, rc;
    double PI25DT = 3.141592653589793238462643;
    double mypi, pi, h, sum, x, a;
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD, &myid);
    if (myid == 0) {
        printf("Enter the number of intervals: (0 quits) ");
        scanf("%d", &n);
    }
    MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
```

Esempio: PI greco in C (2)

```
if (n != 0) {
    h    = 1.0 / (double) n;
    sum  = 0.0;
    for (i = myid + 1; i <= n; i += numprocs) {
        x = h * ((double) i - 0.5);
        sum += 4.0 / (1.0 + x*x);
    }
    mypi = h * sum;
    MPI_Reduce(&mypi, &pi, 1, MPI_DOUBLE, MPI_SUM, 0,
              MPI_COMM_WORLD);
    if (myid == 0)
        printf("pi is approximately %.16f, Error is %.16f\n",
              pi, fabs(pi - PI25DT));
}
MPI_Finalize();
return 0;
}
```

Altre routine...



- Molte routine di broadcast hanno un corrispettivo che permette di maneggiare vettori anzichè scalari
 - `MPI_Gatherv()`, `MPI_Scatterv()`,
`MPI_Allgatherv()`, `MPI_Alltoallv()`
- `MPI_Reduce_scatter()`: funzionalità equivalente a reduce seguita da scatter
- I dettagli riguardanti queste ed altre routine derivate si possono ottenere dal manuale dell'MPI

Derived Datatypes

Send a sub-vector from
process 0 to 1

```
/* spedizione di un sotto-vettore dal processo 0 al processo 1
 *
 *
 * Note: Dovrebbe eseguito su due processi.
 *
 */
#include <stdio.h>
#include "mpi.h"

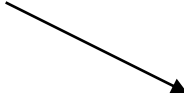
main(int argc, char* argv[]) {
    float vector[100];
    MPI_Status status;
    int p;
    int my_rank;
    int i;

    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &p);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    /* Inizializzazione vettore e spedizione */
    if (my_rank == 0) {
        for (i = 0; i < 50; i++)
            vector[i] = 0.0;
        for (i = 50; i < 100; i++)
            vector[i] = 1.0;
        MPI_Send(vector+50, 50, MPI_FLOAT, 1, 0,
                MPI_COMM_WORLD);
    } else { /* my_rank == 1 */
        MPI_Recv(vector+50, 50, MPI_FLOAT, 0, 0,
                MPI_COMM_WORLD, &status);
        for (i = 50; i < 100; i++)
            printf("%3.1f ", vector[i]);
        printf("\n");
    }

    MPI_Finalize();
} /* main */
```

Possible since elements of
A vector in C are contiguous!



```

/* spedizione della terza colonna di una matrice dal processo 0 al processo 1
 *   process 1
 *
 * Note: Dovrebbe eseguito su due processi.
 */
#include <stdio.h>
#include "mpi.h"

main(int argc, char* argv[]) {
    int p;
    int my_rank;
    float A[10][10];
    MPI_Status status;
    MPI_Datatype column_mpi_t;
    int i, j;

    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    MPI_Type_vector(10, 1, 10, MPI_FLOAT, &column_mpi_t);
    MPI_Type_commit(&column_mpi_t);

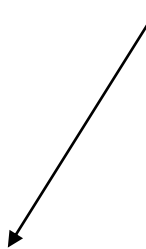
    if (my_rank == 0) {
        for (i = 0; i < 10; i++)
            for (j = 0; j < 10; j++)
                A[i][j] = (float) j;
        MPI_Send(&(A[0][2]), 1, column_mpi_t, 1, 0,
                MPI_COMM_WORLD);
    } else { /* my_rank = 1 */
        MPI_Recv(&(A[0][2]), 1, column_mpi_t, 0, 0,
                MPI_COMM_WORLD, &status);
        for (i = 0; i < 10; i++)
            printf("%3.1f ", A[i][2]);
        printf("\n");
    }

    MPI_Finalize();
} /* main */

```

Send 3rd column from
process 0 to 1

Non contiguous elements
In C matrixes!



Initialization



Process 1 receives and
places the column in its own
A matrix



Send a column 1 to row 1
on another process

Send column

Receive a "10 MPI_FLOAT data
element"

```
/* Interessante: spediamo la colonna 1 di una matrice
 * alla riga 1 di una matrice (su un altro processo)
 *
 *
 * Note: Dovrebbe eseguito su due processi.
 */
#include <stdio.h>
#include "mpi.h"

main(int argc, char* argv[]) {
    int p;
    int my_rank;
    float A[10][10];
    MPI_Status status;
    MPI_Datatype column_mpi_t;
    int i, j;

    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    MPI_Type_vector(10, 1, 10, MPI_FLOAT, &column_mpi_t);
    MPI_Type_commit(&column_mpi_t);

    if (my_rank == 0) {
        for (i = 0; i < 10; i++)
            for (j = 0; j < 10; j++)
                A[i][j] = (float) i;
        MPI_Send(&A[0][0], 1, column_mpi_t, 1, 0,
                MPI_COMM_WORLD);
    } else { /* my_rank = 1 */
        for (i = 0; i < 10; i++)
            for (j = 0; j < 10; j++)
                A[i][j] = 0.0;
        MPI_Recv(&A[0][0], 10, MPI_FLOAT, 0, 0,
                MPI_COMM_WORLD, &status);
        for (j = 0; j < 10; j++)
            printf("%3.1f ", A[0][j]);
        printf("\n");
    }

    MPI_Finalize();
} /* main */
```

Initialization

Send 3rd row from process 0 to 1 (no use of derived datatypes)

```
/* Spedisco la terza riga di una matrice dal processo 0
 * al processo 1
 * NB Non c'e' bisogno di utilizzare i derived datatypes!

 * Note: Dovrebbe eseguito su due processi.
 */
#include <stdio.h>
#include "mpi.h"

main(int argc, char* argv[]) {
    int p;
    int my_rank;
    float A[10][10];
    MPI_Status status;
    int i, j;

    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    if (my_rank == 0) {
        for (i = 0; i < 10; i++)
            for (j = 0; j < 10; j++)
                A[i][j] = (float) i;
        MPI_Send(&(A[2][0]), 10, MPI_FLOAT, 1, 0,
                MPI_COMM_WORLD);
    } else { /* my_rank = 1 */
        MPI_Recv(&(A[2][0]), 10, MPI_FLOAT, 0, 0,
                MPI_COMM_WORLD, &status);
        for (j = 0; j < 10; j++)
            printf("%3.1f ", A[2][j]);
        printf("\n");
    }

    MPI_Finalize();
} /* main */
```

Placed in third row, but can go anywhere!!!



Send the upper triangle of a matrix from 0 to 1

```
/* Interessante: Spedisce la porzione triangolo superiore
 * di una matrice da 0 a 1
 *
 * Note: Dovrebbe eseguito su due processi.
 */
#include <stdio.h>
#include "mpi.h"

#define n 10

main(int argc, char* argv[]) {
    int p;
    int my_rank;
    float A[n][n];          /* Complete Matrix */
    float T[n][n];          /* Upper Triangle */
    int displacements[n];
    int block_lengths[n];
    MPI_Datatype index_mpi_t;
    int i, j;
    MPI_Status status;

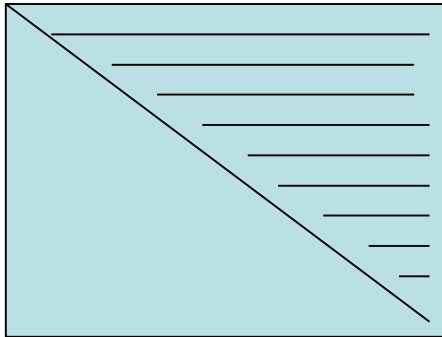
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &p);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);

    for (i = 0; i < n; i++) {
        block_lengths[i] = n-i;
        displacements[i] = (n+1)*i;
    }
    MPI_Type_indexed(n, block_lengths, displacements,
        MPI_FLOAT, &index_mpi_t);
    MPI_Type_commit(&index_mpi_t);

    if (my_rank == 0) {
        for (i = 0; i < n; i++)
            for (j = 0; j < n; j++)
                A[i][j] = (float) i + j;
        MPI_Send(A, 1, index_mpi_t, 1, 0, MPI_COMM_WORLD);
    } else { /* my_rank == 1 */
        for (i = 0; i < n; i++)
            for (j = 0; j < n; j++)
                T[i][j] = 0.0;
        MPI_Recv(T, 1, index_mpi_t, 0, 0, MPI_COMM_WORLD, &status);
        for (i = 0; i < n; i++) {
            for (j = 0; j < n; j++)
                printf("%4.1f ", T[i][j]);
            printf("\n");
        }
    }

    MPI_Finalize();
} /* main */
```

The trick is here! Locate the various Rows of the triangle!



i